

Answers to Revision Exercises

N1.1

- 1 a Nigeria b 1.08×10^8 c 4.2×10^7
 2 a 15 b 525
 3 i 360000 ii 0.0029
 4 $2^2 \times 5 \times 7$
 5 a $7p$ b $i xy$ ii x^2y^2
 6 4.3×10^3
 7 a 5.72×10^6 b 1.4×10^{-7}
 8 a 5.4×10^{-11} b 3.67×10^{-20}

- 3 a i 2^7 ii 3^6 b 0
 4 a $2^{\frac{3}{2}}$ b $9^{\frac{1}{4}}$ c $2^{-2.5}$
 5 46
 6 a i 1 ii $\frac{1}{25}$ iii $\frac{1}{3}$ iv 5 b $\frac{2-k}{2}$
 7 $\frac{7}{2}$
 8 a 4 b $2\sqrt{10}$ c 81.3%
 9 a 6 b $\frac{1}{4}$
 10 $-3 \pm \sqrt{13}$

- 11 a 3^4 b $2^{-3} \times 5^2$

N2

- 1 411
 2 a 0.08717948718 b 0.087
 3 a 55.25 b 0.882
 4 a $\frac{31}{40}$ b $2\frac{11}{12}$
 5 $\frac{7}{24}$
 6 a 9.719 11.710 b 10 since both bounds agree
 7 a 1.75 1.65 31.05 30.95 b 29.2 c 5531

N6

- 1 a 10 b $\frac{v^2}{2g}$
 2 a 27.22 b 27
 3 a $1\frac{1}{3}$ b $2\frac{9}{10}$
 4 8.09
 5 21
 6 17
 7 2.00
 8 22.8
 9 a $2 + 3 \times 4$ b $(2 + 3) \div 4$ c $2 \div 3 \times 4$

N3

- 1 11%
 2 a $\frac{4}{5}$ b $3\frac{1}{5}$
 3 172
 4 a 62.9 b 65
 5 $\frac{23}{99}$
 6 a i 9 ii multiple of 5 b 1.4 to 2 s.f.
 7 $\frac{23}{45}$
 8 $2\frac{11}{12}$
 9 $\frac{31}{15}$

N7

- 1 i $B \subset A$ ii $a \cap B = \emptyset$
 2 a $7-x$ b 3
 3 a i 5 ii 7 iii 9 b i 3 ii 15 iii 0
 4 a 11, 12, 13, 15 b 0
 c No, 11 is not a multiple of 3
 5 a i - ii e.g. 5, 10, 20 b i - ii e.g. 15, 45, 75
 6 a Kitchen chairs b i 1, 2, 3, 4, 5, 6, 7, 8, 9,
 ii Yes P all even
 7 both in P but not intersecting

N4

- 1 200 150 225 150 10
 2 9
 3 704
 4 600
 5 a 150 b 320
 6 a 7.5 b 95
 7 a Mars b 1:30
 8 $\frac{1}{4}$
 9 a 5062.50 b 0.4096

- 1 14 300
 2 24
 3 264
 4 a 138.2 b -
 5 a 42 b 630
 6 576
 7 151
 8 116
 9 95.5

N5

- 1 a $\frac{1}{8}$ b $\frac{3}{7}$ c $\frac{9}{64}$
 2 a $3\sqrt{2}$ b $\frac{\sqrt{2}}{32}$

- 1 55
 2 15
 3 $50 + x$
 4 36

- 5** 15
6 a i 61 ii cyclic quadrilateral
 b 29
7 144
8 a i 55 ii same arc
 b i 85 ii Cyclic quadrilateral
 c No, subtended angle $\neq 90^\circ$
9 71
10 28

- S3**
1 a Enlargement Scale factor 3 about (1, 2)
 b triangle at (1, 6) (3, 6) (3, 7)
2 a triangle at (2, 6) (0, 6) (2, 10)
 b triangle at (6, 3) (6, 4) (8, 3)
3 a Rotation, 90° clockwise about (2, 0)
 b FTTF
4 No
5 a 49 b i 3.75 ii 1
6 a 3.5 b 2.7
7 a 0.162 b 43200
8 a 6.5 b 8320
9 a $1:\sqrt{k}$ b 7.1
10 8

- S4**
1 7.22
2 a 30 b 10.2
3 0.3096
4 a - b 1.58
5 5.74 (2 d.p.)
6 4

- S5**
1 a 290 b 146
2 -
3 -
4 -
5 -
6 232.4
7 17.6
8 a 5.66 b 38.9 c 33.6
9 a 335 b 104.5
10 27.6

- S6**
1 23.9
2 1.31
3 a 12.6 b 2.6
4 15
5 15π
6 a i $\frac{1}{3}\pi x^2$ ii $\frac{2\pi x}{3}$ b 27
7 a 128π b 112π
8 a 21.8 b 66.4

- S7**
1 (7, -1)
2 a $\begin{pmatrix} 4 \\ 3 \end{pmatrix}$ b $\begin{pmatrix} -4 \\ 1 \end{pmatrix}$
3 a $\begin{pmatrix} 5 \\ 2 \end{pmatrix}$ b i $k\begin{pmatrix} 5 \\ 2 \end{pmatrix}$ ii $\begin{pmatrix} -1+5k \\ -2+2k \end{pmatrix}$ iii $\begin{pmatrix} 4-5k \\ -2k \end{pmatrix}$
 c 0.5 d $k = \frac{1}{2} \rightarrow x$ midpoint of OB
4 a i $-a+b$ ii $2a$ iii $-2a+2b$
 b parallel, $QR = 2MN$
5 a i $a + \frac{1}{2}b$ ii $b + \frac{1}{2}a$ iii $-a+b$
 b $\overline{XY} = \frac{1}{2}(b-a) = \frac{1}{2}\overline{QS}$

- 6** a i $-6a+6b$ ii $6a$ b $12b-3a$
 c $\overline{EY} = \frac{4}{3}\overline{EX}$ and E common
7 -
8 i $\begin{pmatrix} 3 \\ 2 \end{pmatrix}$ ii $\begin{pmatrix} 5 \\ 10 \end{pmatrix}$
9 a $2a+4c$ b $\overline{OM} = \frac{3}{2}\overline{OP}$ and O common

- S8**
1 a 57.6 b 2 c 80
2 1.79
3 3.156990642
4 a i (90, 1) ii (180, 0) b i (45, 0) ii (90, -3)
5 $A = 2$, $k = 6$
6 a i $\frac{1}{2}$ ii $-\frac{1}{2}$ b i 114, 246 ii 41, 319

- D1**
1 a 2 b B more consistent,
 B higher median so on
 average better
2 9.5
3 a i 16 ii 17.5 iii 17.3
 b i up
 ii New student age > original mean value
4 a 4 b 5, 5, 8 c e.g. 4, 5, 7, 7
5 a 1.8
 b $p = q$, equal number of values in each list

- D2**
1 a 28, 50, 64, 74, 80 b - c 14
2 a i 42 ii 10 b 28
3 a 74 b 22 c 20 d 7
4 a 3, 13, 30, 60, 81, 88, 90 b - c 37 d 64

- D3**
1 a 18 b 12
2 0.16
3 0.4
4 a 0.3 b 170

- 5** a i 0.9 ii 0.1 b i 0.09 ii 0.48
6 $\frac{91}{216}$
7 $\frac{29}{45}$
8 $\frac{660}{1000}$
9 $\frac{26}{56}$

- D4**
1 Heights of bars in the ratio: 1, 4, 1.6
2 a 120, 72 b -
3 348
4 a bar heights: 1, 4, 2.8, 0.4 b 9
5 a i - ii 130, 120 b 2500

- D5**
1 a $\frac{1}{6}$ b $\frac{7}{18}$
2 a 32 b 21
3 a - b $\frac{7}{18}$ c $\frac{25}{36}$
4 -
5 a No b - c i $\frac{1}{36}$ ii $\frac{11}{36}$
6 a - b $\frac{3}{28}$

- A1**
1 a $6t+10$ b $y^3 - 3y^2$ c $x^2 + 10x + 21$ d p^7q^8
2 a $12x^2 + x - 35$ b $8p^{12}$ c $16y^4$
3 a k^3 b i $6x-1$ ii $x^2 + 5xy + 6y^2$
 c $(p+q)(p+q+5)$ d m^8 e $6t^6r^3$
4 -
5 a $2x(5x-1)$ b $(x+3)(x-3)$ c $(3x-1)(x-4)$
6 -
7 $(3x-1)(3x-1)$
8 a $x(x+1)$ b $(y+5)(y-7)$

- A2**
1 a $6x, 4(x+7)$ b i $4x+28=6$ ii 14

- 2** -1.5
3 $\frac{x-4}{2x-3}$
4 a $9x-5$ b 6
5 a $-6x+23$ b $32x^5y^{15}$ c $\frac{2(n-1)}{n-2}$
6 a 7 b $\frac{2x}{2x+3}$
7 0.75
8 $\frac{4}{5}$
9 $\frac{3}{x+4}$

- A3**
1 $4n+6$
2 i add 3 more every time
 ii difference are consecutive square numbers
3 a -4 b 14 c $3n+5$
4 a 17, 27 b 10
5 1.12 or -1.79
6 a $4n-1$ b Yes, 80th term
7 a $n^2 - (n-1)(n+1)$ b 1
8 i $(x-3)(x-4)$ ii 3, 4
9 a - b i $-\frac{13}{3}, \frac{3}{2}$ ii 8
10 $-\frac{1}{2}, \frac{3}{2}$

- A4**
1 $x < 1.5$
2 a $y = 2x-4$ b -
3 region bounded by the three lines
4 region bounded by the three lines
5 -2, -1, 0, 1, 2, 3
6 $y = 4x+5$
7 $y = 2x+6$
8 $y = -2x+5$
9 $6 < x \leq 9$
10 $y = 2x-4$
11 i $\frac{5}{3}$ ii $(0, -2)$
12 C E A D B

- A5**
1 $\frac{1}{m} + u$
2 lh^2
3 $\sqrt{\frac{A}{\pi} + r^2}$
4 $\frac{cp}{q-p}$
5 Show that $(2n+1)^2 + (2m+1)^2 = 4(n^2 + n + m) + 2$
6 Yes
7 a 5n
 b i $5n+5(n+1) = 10n+5 = \text{even} + \text{odd} = \text{odd}$
 ii $5n \times 5(n+1) = 25n(n+1) = \text{odd} \times \text{even} = \text{even}$
8 Show it simplifies to 4n
9 a 60 b $\frac{200p-20}{3}$ c $\frac{240+36w}{180-3w}$
10 e.g. $6 \times 13 - 1 = 77 \times 11$

- A6**
1 $\frac{5}{3}, -1$
2 a $-2 \leq x \leq 2$ b -
3 a $(5-x)^2 + (6-x)^2 = (x+4)^2$ b 1.58



4 $\left(\frac{4}{5}, \frac{22}{5}\right)$ and $(4, -2)$

5 a $\left(\frac{1}{2}, 1\right)$ b $\left(\frac{1}{2}, 1\right)$

6 a - b $23.5, -8.5$

7 a $y = 2x + 3$ b $(0.5, 0.5)$

8 $(5.5, 14)$

A7

1 a 36, 56, 48, 20 b - c 60.5

2 a i $(0, 9)$ ii $(8, 25)$ -

3 a - b i 1.42 or -8.42 ii 13.68

4 a $x^2 = \sqrt{-9}$, not possible b $(3, 4)$ or $\left(-\frac{7}{5}, \frac{24}{5}\right)$

5 250

A8

1 Line through $(0, -2)$ and $(2, 8)$

2 a 5, -1, b - c -1.25

3 a 2.125, -1 b -

4 i H ii D iii A

5 a 5.4, 3.3, 3, 4.5 b - c $0.6, 3.4$

d $y = 7 - x$

6 a 0.25, 2.5, 8, 15.25 b - c 1.4

d 2.5

A9

1 36

2 50

3 7.2

4 D A B C

5 a $x = 4.9t^2$ b 44.1 c 1.43

6 a i $R = \frac{3.6}{r^2}$ ii - b 0.4

7 a 24 84 b Home c 0 and 40
d 15 e 84

A10

1 a i $\frac{3}{2}$ ii $\frac{3}{4}$ b 1

c i x ii $f(x) = f^{-1}(x)$

2 a $-1 \leq f(x) \leq 1$ b $p = 0$ $q = 45$

3 a 3 b $-0.9, 2.5$ c -13 d 3.8

e $2 < k < 7$

4 $x = 10$ or 3

5 a -11 b 4 c 4 d $x < 0$
e $(x - 1)^2$

A11

1 a $5000 - 1250x$ b $(4, 10000)$

c i Maximum

d i 4 ii Maximum profit

2 a $3x^2 - 12$ b -12

c $A(-2, 43) B(2, 1)$

3 $40t^3$

4 a $3t^2 + 4t - 5$ b 20

5 a $x(28 - 2x)$ b i $28 - 4x$ ii 7

c 98 iii graph is \cap shaped

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