

S7

Space exam review

1 A is the point with coordinates (2, 3).

$$\vec{AB} = \begin{pmatrix} 5 \\ -4 \end{pmatrix}.$$

Find the coordinates of B.

(.....,))

(Total 2 marks)

2

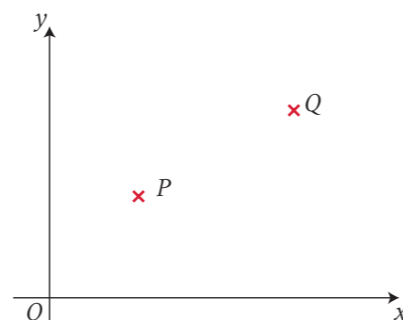


Diagram **NOT** accurately drawn

The diagram is a sketch.

P is the point (2, 3)

Q is the point (6, 6)

a Write down the vector \vec{PQ}

Write your answer as a column vector $\begin{pmatrix} x \\ y \end{pmatrix}$

$\begin{pmatrix} \\ \end{pmatrix}$
.....
(2)

PQRS is a parallelogram.

$$\vec{PR} = \begin{pmatrix} 4 \\ 7 \end{pmatrix}$$

b Find the vector \vec{QS}

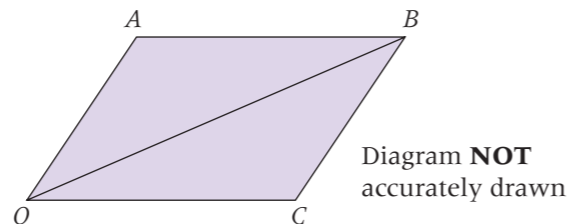
Write your answer as a column vector $\begin{pmatrix} x \\ y \end{pmatrix}$

$\begin{pmatrix} \\ \end{pmatrix}$
.....

(2)

(Total 4 marks)

3 OABC is a parallelogram.



$$\vec{OA} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}, \vec{OC} = \begin{pmatrix} 4 \\ 0 \end{pmatrix}$$

a Find the vector \vec{OB} as a column vector.

$\begin{pmatrix} \\ \end{pmatrix}$
..... (1)

X is the point on OB such that $OX = kOB$, where $0 < k < 1$

b Find, in terms of k, the vectors

i \vec{OX} ,
.....

ii \vec{AX} ,
.....

iii \vec{XC} .
..... (3)

c Find the value of k for which $\vec{AX} = \vec{XC}$.

..... (2)

d Use your answer to part **c** to show that the diagonals of the parallelogram OABC bisect one another.

.....
.....
..... (2)

(Total 8 marks)

4 PQR is a triangle.

M and N are the midpoints of PQ and PR respectively.

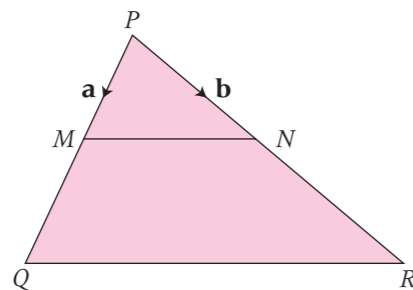


Diagram **NOT** accurately drawn

$\vec{PM} = \mathbf{a}$ $\vec{PN} = \mathbf{b}$.

a Find, in terms of \mathbf{a} and/or \mathbf{b} ,

i \vec{MN}

.....

ii \vec{PQ}

.....

iii \vec{QR}

.....

(3)

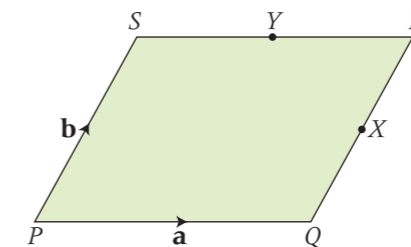
b Use your answers to a i and iii to write down two geometrical facts about the lines MN and QR .

.....

(2)

(Total 5 marks)

5



$PQRS$ is a parallelogram.

X is the midpoint of QR and Y is the midpoint of SR .

$\vec{PQ} = \mathbf{a}$ and $\vec{PS} = \mathbf{b}$.

a Write down, in terms of \mathbf{a} and \mathbf{b} , expressions for

i \vec{PX}

.....

ii \vec{PY}

.....

iii \vec{QS}

.....

(3)

b Use a vector method to show that XY is parallel to QS and that $XY = \frac{1}{2}QS$.

(2)

(Total 5 marks)

6

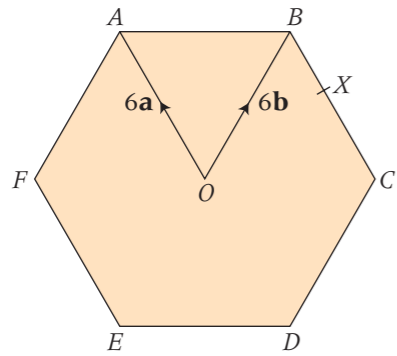


Diagram **NOT** accurately drawn

The diagram shows a regular hexagon $ABCDEF$ with centre O .

$\vec{OA} = 6\mathbf{a}$ $\vec{OB} = 6\mathbf{b}$

a Express in terms of \mathbf{a} and/or \mathbf{b}

i \vec{AB} ,

.....

ii \vec{EF} .

.....

(2)

X is the midpoint of BC .

b Express \vec{EX} in terms of \mathbf{a} and/or \mathbf{b}

.....

(2)

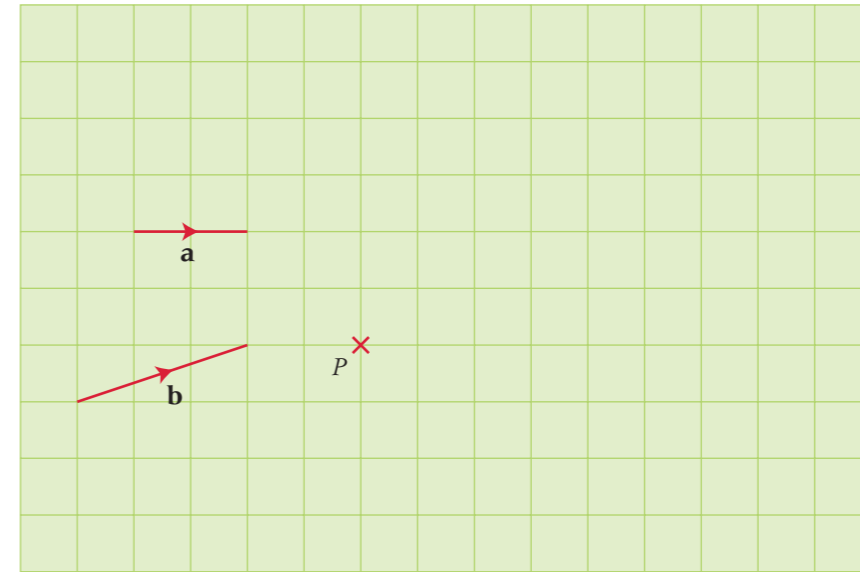
Y is the point on AB extended, such that $AB : BY = 3 : 2$

c Prove that E, X and Y lie on the same straight line.

(3)

(Total 7 marks)

7



The diagram shows two vectors \mathbf{a} and \mathbf{b} .

$\vec{PQ} = \mathbf{a} + 2\mathbf{b}$

On the grid above draw the vector \vec{PQ} .

(Total 2 marks)

8 $\mathbf{p} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$ and $\mathbf{q} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$

Write down as a column vector

i $\mathbf{p} - \mathbf{q}$

$\begin{pmatrix} \\ \end{pmatrix}$

.....

ii $3\mathbf{p} + \mathbf{q}$

$\begin{pmatrix} \\ \end{pmatrix}$

.....

(Total 2 marks)

9

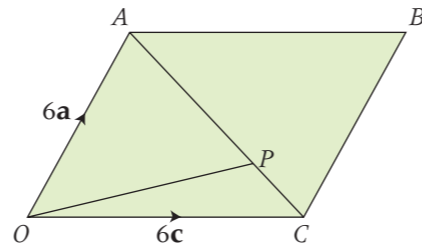


Diagram **NOT** accurately drawn

$OABC$ is a parallelogram.

P is the point on AC such that $AP = \frac{2}{3}AC$.

$\vec{OA} = 6\mathbf{a}$. $\vec{OC} = 6\mathbf{c}$.

a Find the vector \vec{OP} .

Give your answer in terms of \mathbf{a} and \mathbf{c} .

..... (3)

The midpoint of CB is M .

b Prove that OPM is a straight line.

(2)

(Total 5 marks)